Some recent results in algebraic graph theory

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Abstract

The rank of a graph G is defined to be the rank (over \mathcal{R}) of its adjacency matrix. In the first part of the talk, we consider the following problem: What is the structure of a connected graph with rank 4? In this talk, we resolve this question by completely characterizing graphs G whose adjacency matrix has rank 4. Given a graph G on nvertices and a field F, the maximum nullity of G over F, denoted by $M^F(G)$, is the largest possible nullity over all $n \times n$ symmetric matrices over F whose (i, j)th entry (for $i \neq j$) is nonzero whenever ij is an edge in G and is zero otherwise. The maximum nullity problem of a graph G is to determine $M^F(G)$. In 2008, the AIM Minimum Rank–Special Graphs Work Group introduced a new graph parameter Z(G), the zero forcing number, to bound $M^F(G)$ from above. The authors posted the following question: What is the class of graphs G for which $Z(G) = M^F(G)$ for some field F? In the second part of this talk, selected recent results on the question will be presented. If time permits, I'll also sketch our work done on the rank of a cograph. This talk is based on joint papers with Prof. Gerard J. Chang (National Taiwan University) and Dr. Liang-Hao Huang (National Central University).